

A quantitative approach to reduce the residual stresses and distortion in additively manufactured parts

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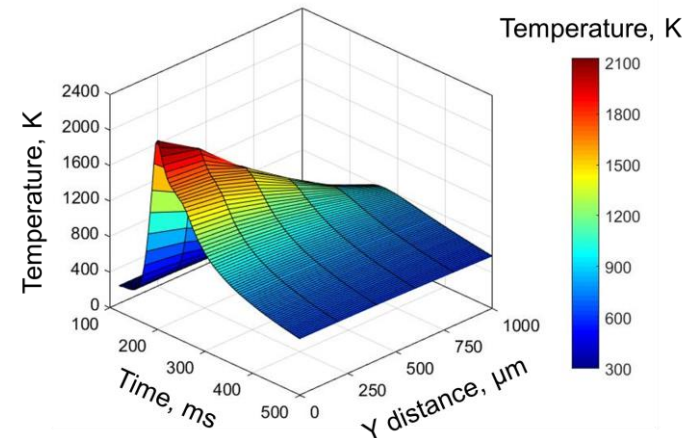
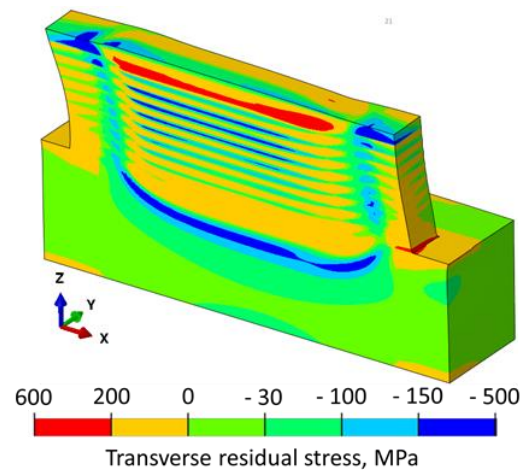
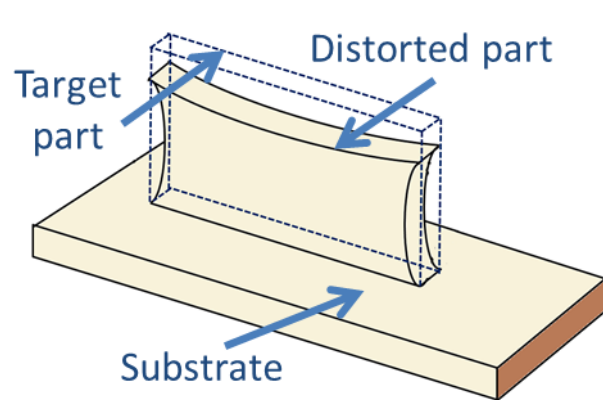
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Why distortion and residual stresses in additive manufacturing ?

Calculation of accurate distortion and residual stress fields

Susceptibility of different alloys to distortion and residual stresses



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Main objectives

Estimation of accurate residual stresses and distortion

- => Dimensional inaccuracy
- => Delamination, buckling, warping
- => Affect mechanical properties

Understand the relative susceptibility of different alloys to distortion

- => Printability of different alloys

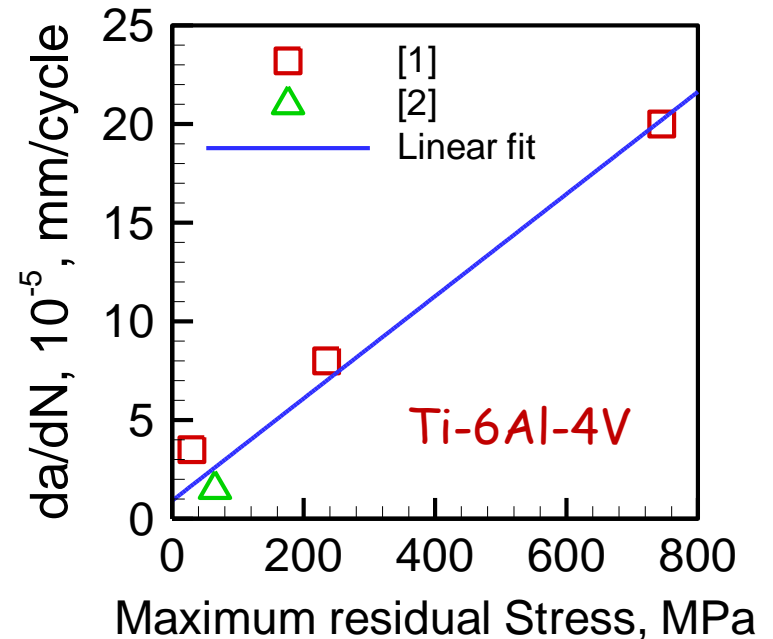
Approach:

3D transient thermo-mechanical model

- => Transient temperature and the velocity field
- => Stresses and strain fields

Analytical method with non-dimensional no.

- => Compare the thermal distortion for different alloys



[1] Leuders et al. Int. J. Fatigue. 2013

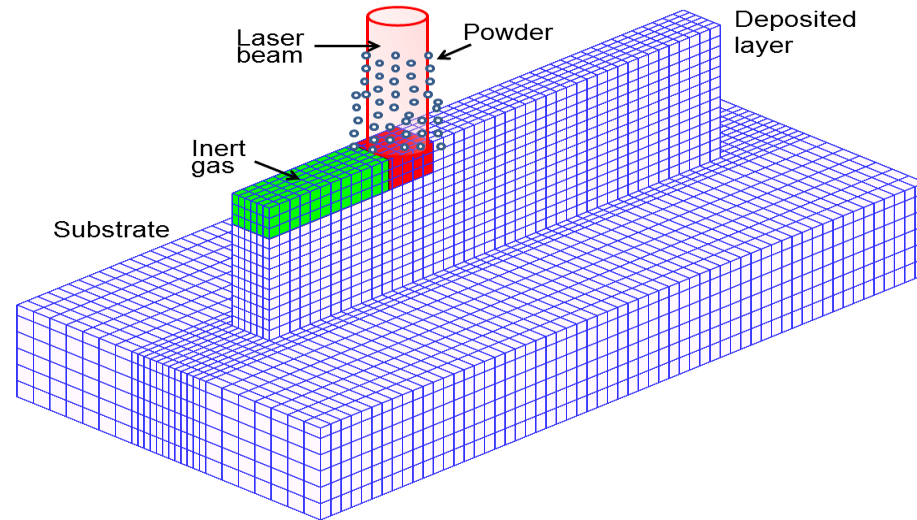
[2] Edwards et al. J. Manuf. Sci. Eng. 2013

Heat transfer and fluid flow model

Solve equations of conservation of mass, momentum and energy

INPUT

Process parameters
Material properties



OUTPUT

Transient
temperature &
velocity fields,
solidification
parameters ...

Calculation domain: about 250,000 cells

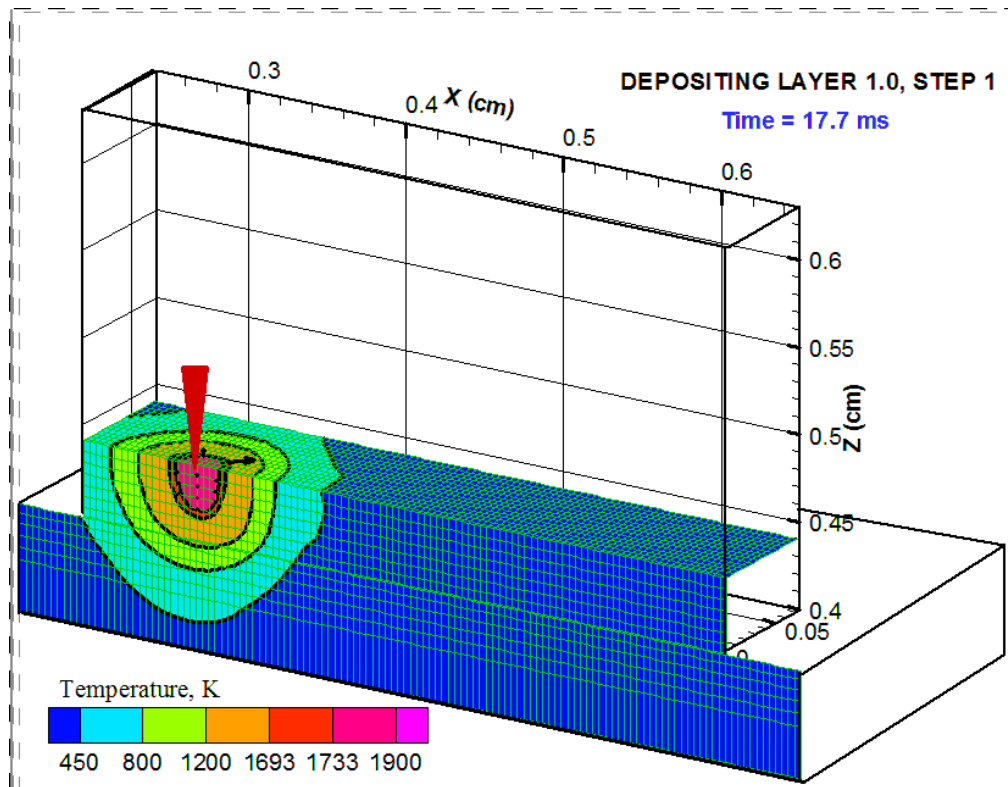
Five main variables: three components of velocities, pressure & enthalpy

1.25 million algebraic equations (250000×5)

100 iteration at any time step => 0.125 billion equations/time step

1000 time step => 125 billion total equations

3D transient temperature distribution



Laser power (W)	Beam radius (mm)	Scanning speed (mm/s)	Layer thickness (mm)	Substrate thickness (mm)
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210

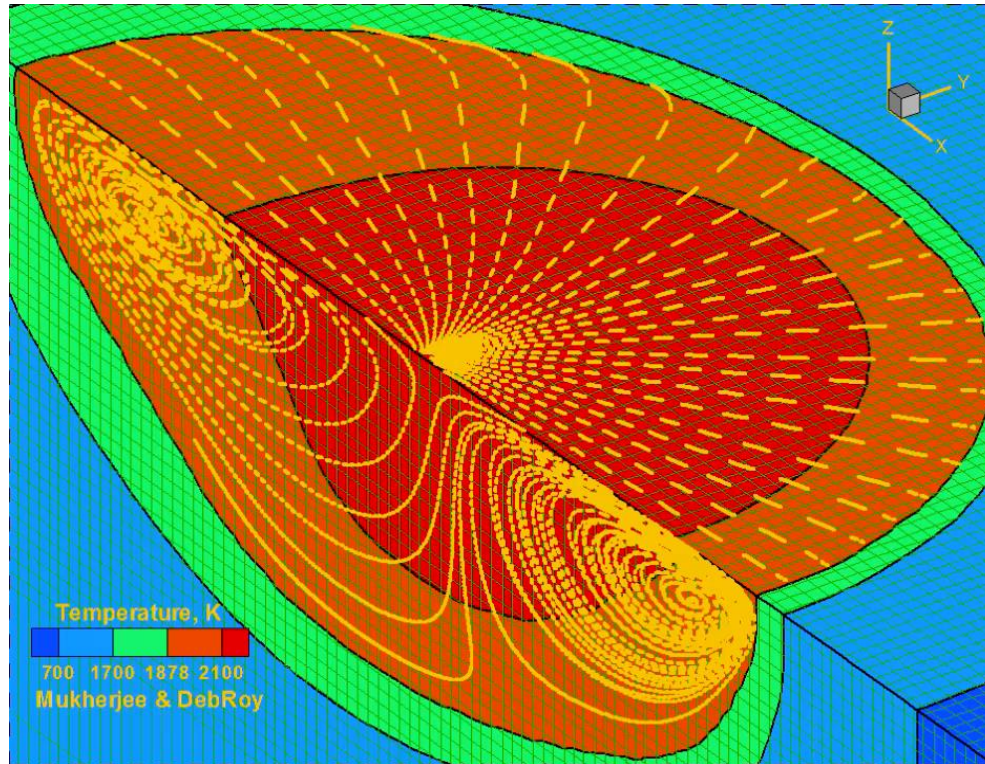
0.5

12.5

0.38

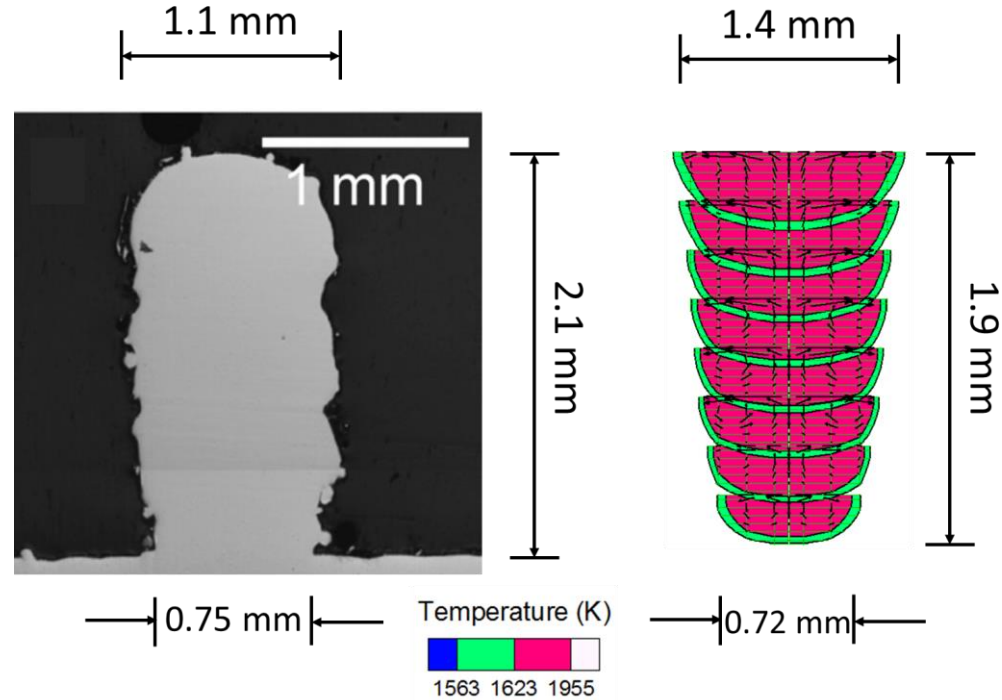
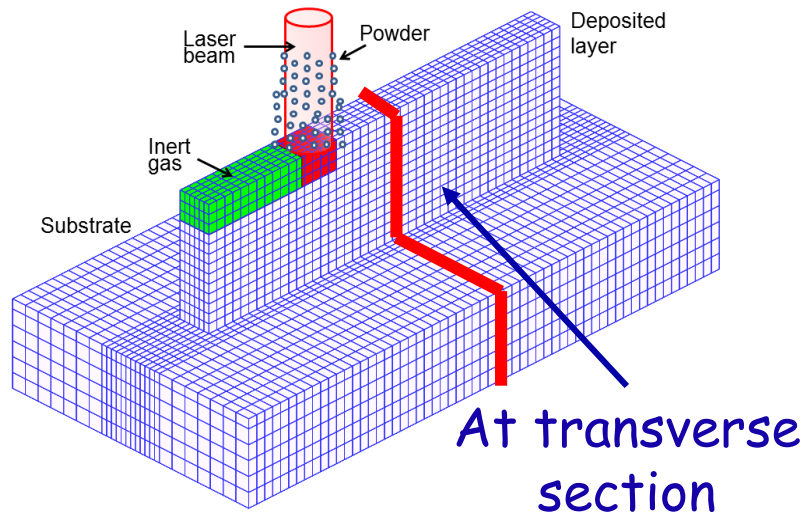
4

3D transient molten metal velocity field



Laser power (W)	Beam radius (mm)	Scanning speed (mm/s)	Layer thickness (mm)	Substrate thickness (mm)
210	0.5	12.5	0.38	4

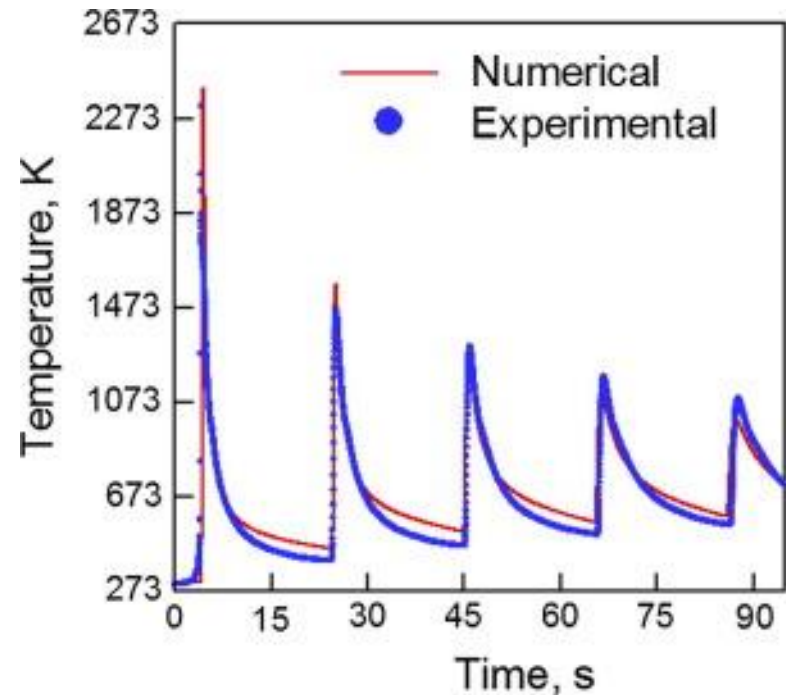
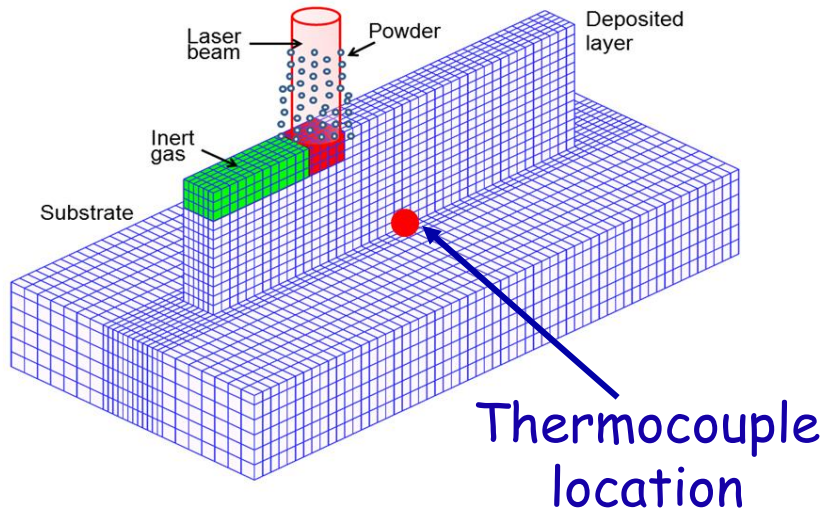
Experimental validation: Shape and size of deposition



Material	Laser power (W)	Beam radius (mm)	Scanning speed (mm/s)	Layer thickness (mm)	Substrate thickness (mm)
IN 625	600	0.5	7.5	0.25	7

Mukherjee et al. Sci. Rep. 2016
www.nature.com/articles/srep19717

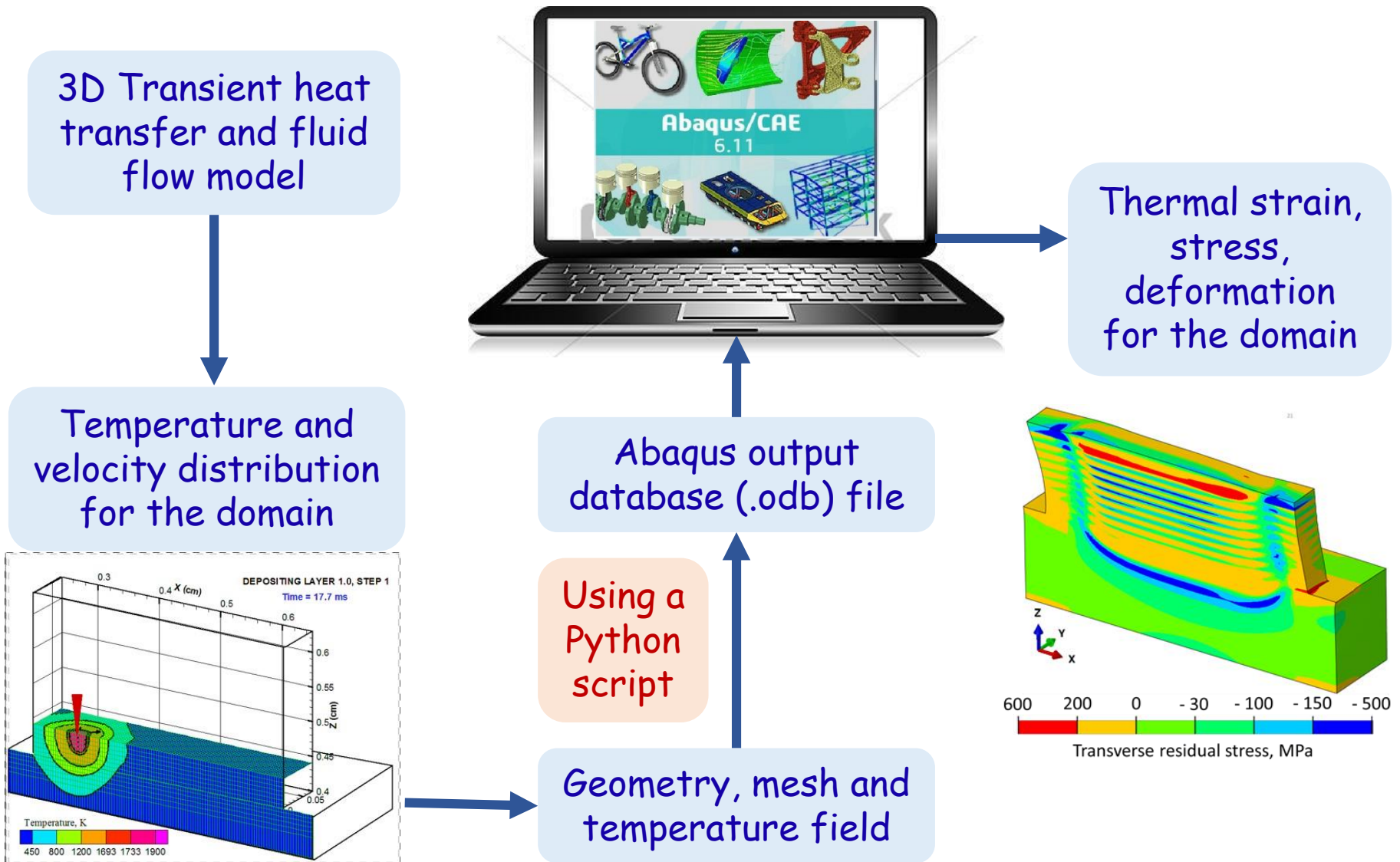
Experimental validation: Thermal cycle



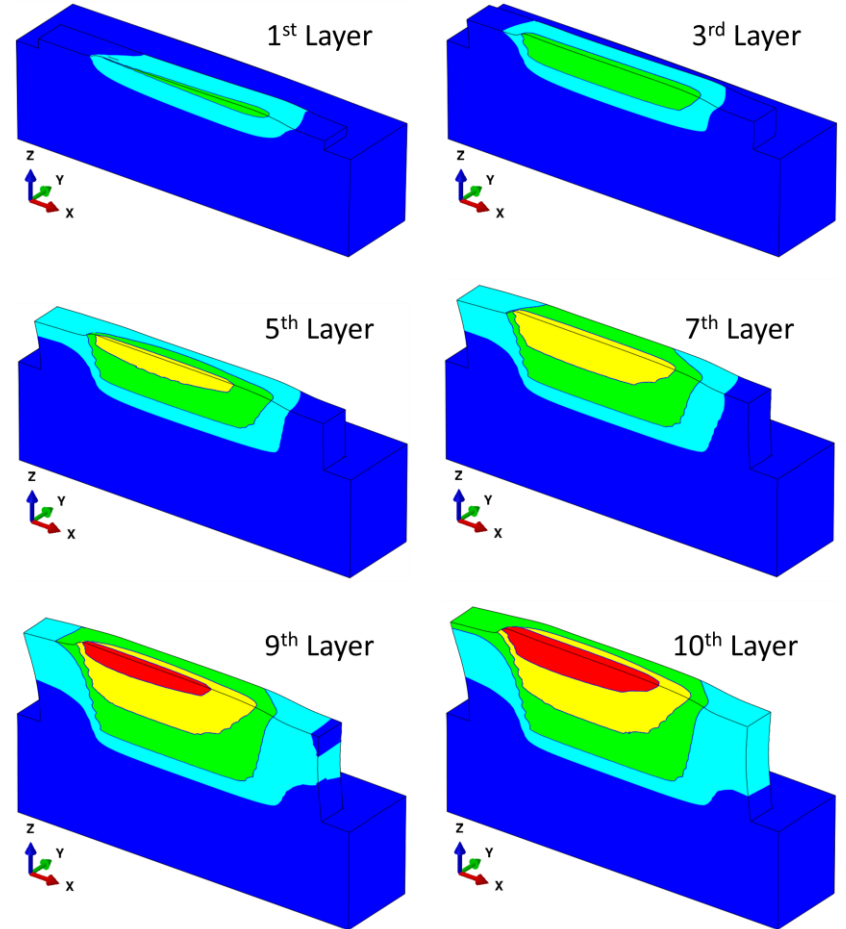
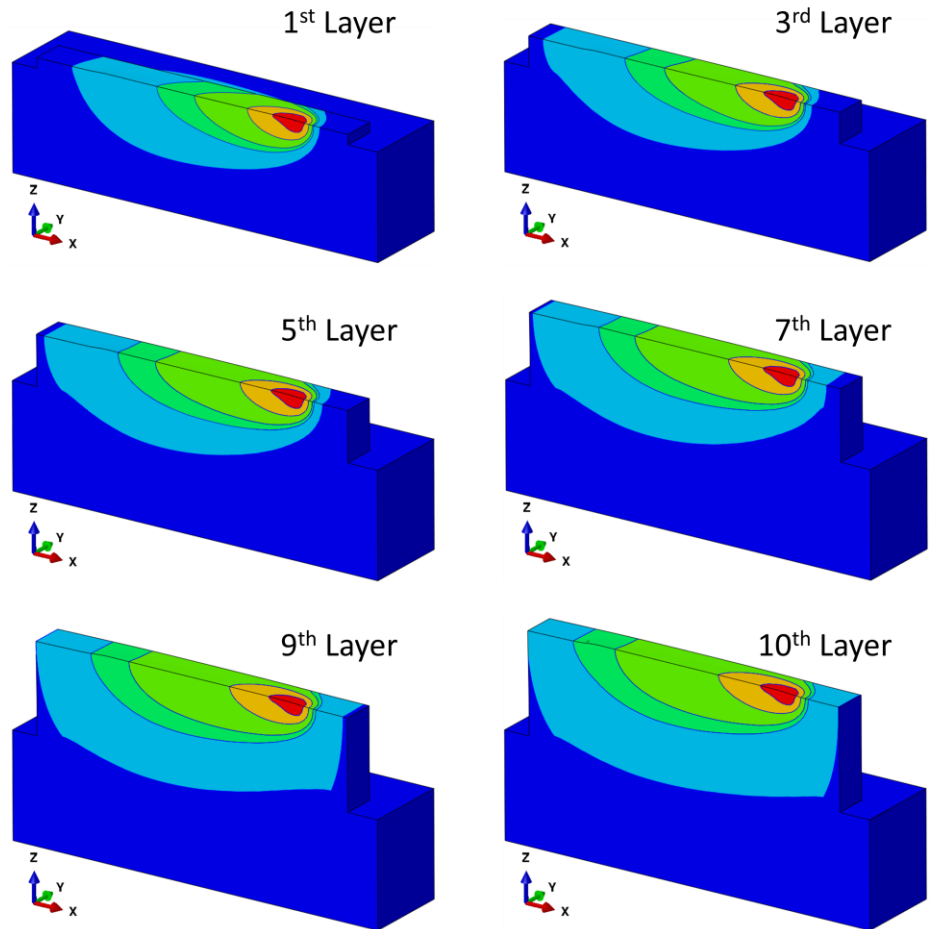
Liquidus temperature = 1878 K

Material	Laser power (W)	Beam radius (mm)	Scanning speed (mm/s)	Layer thickness (mm)	Substrate thickness (mm)
Ti-6Al-4V	2000	1.5	10.6	0.9	10

Calculation of distortion and residual stresses



Calculated thermal strain from temperature field



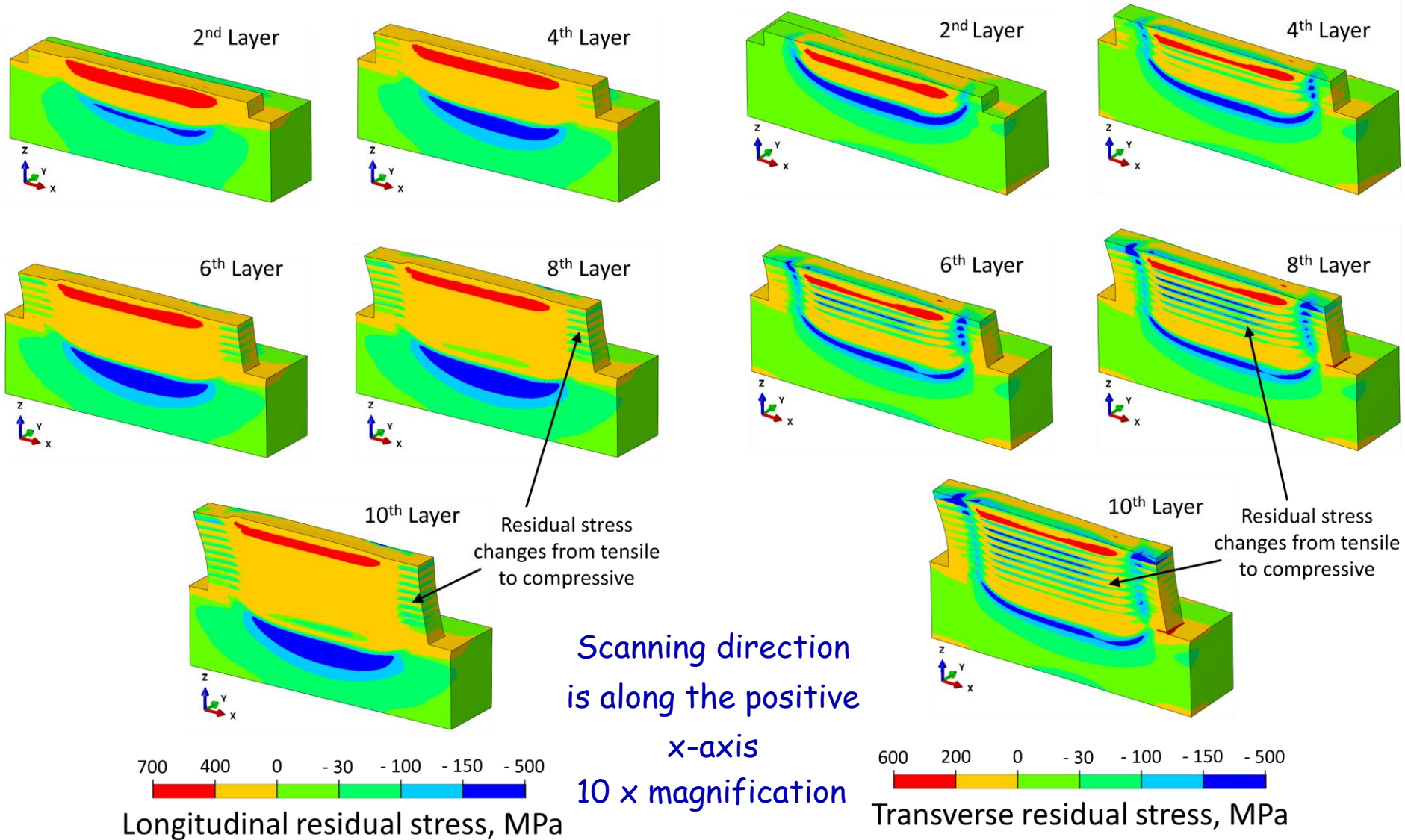
Alloy: Inconel 718, Laser power:
300 W, Speed: 15 mm/s

Mukherjee et al. Comput. Mater. Sci. 2017.

Scanning direction is along the
positive x-axis

10 x magnification

Calculated residual stresses

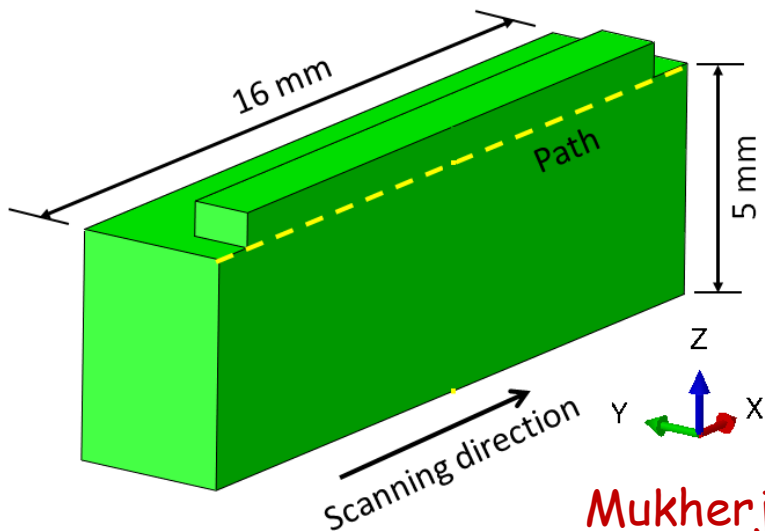
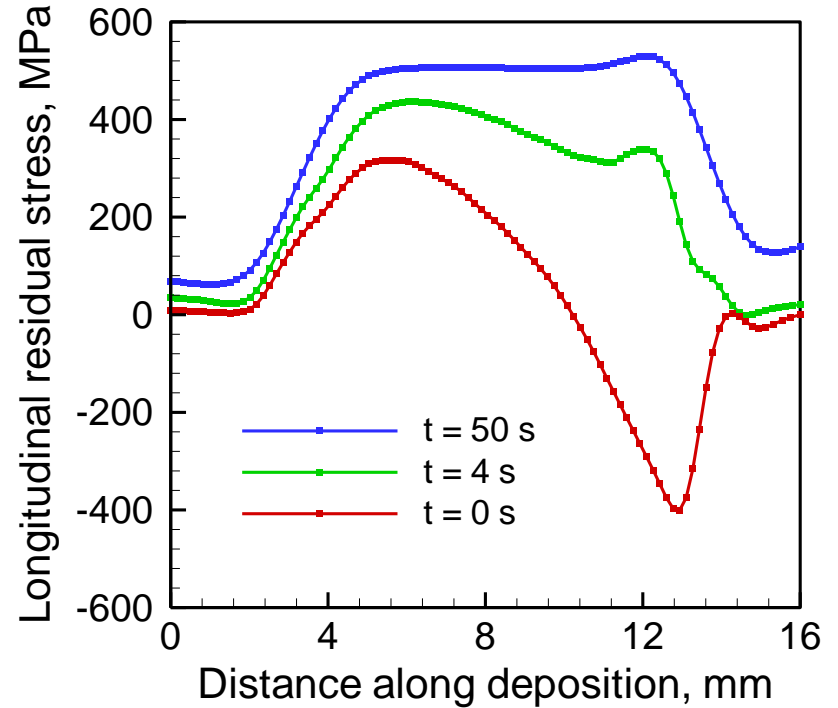
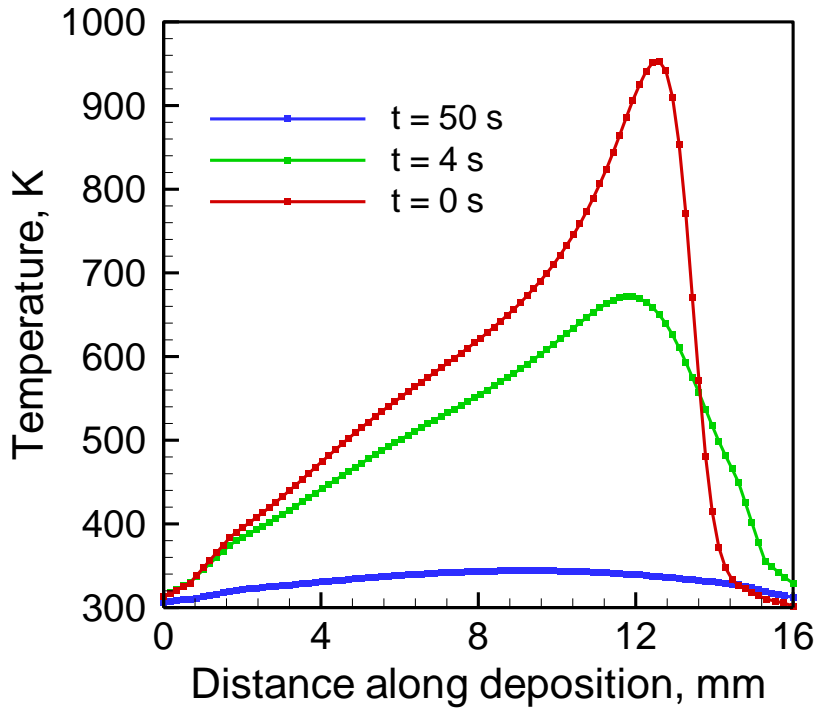


Alloy: Inconel 718,

Laser power: 300 W,

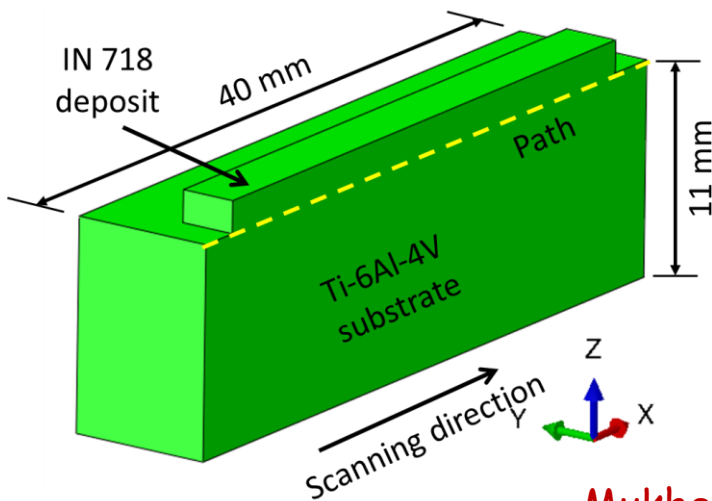
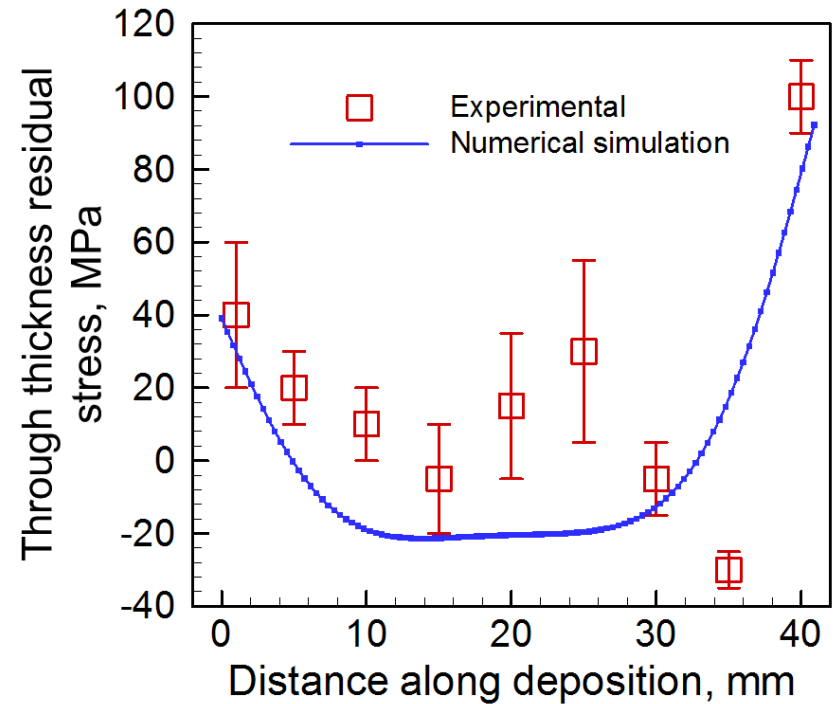
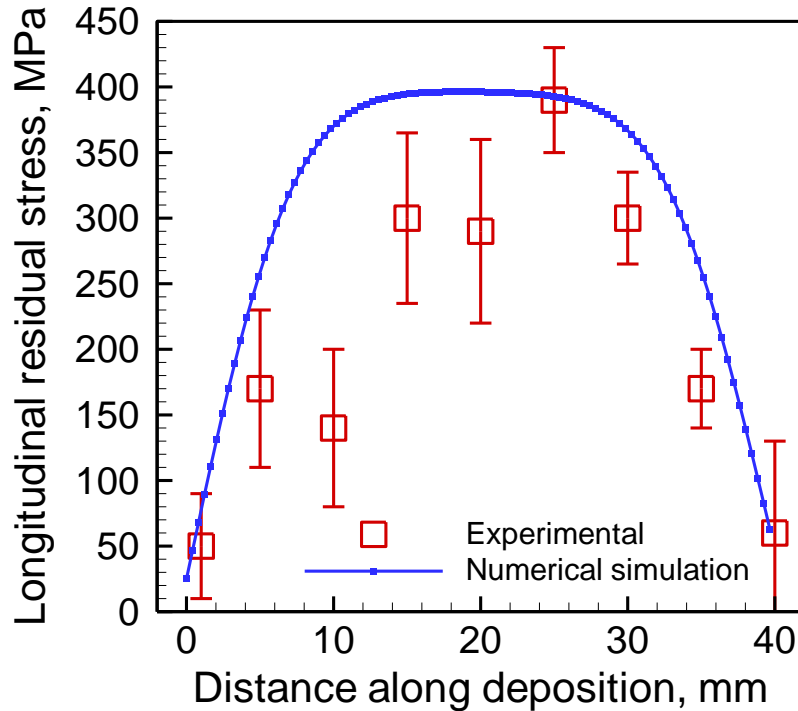
Speed: 15 mm/s

How residual stresses evolve during cooling?



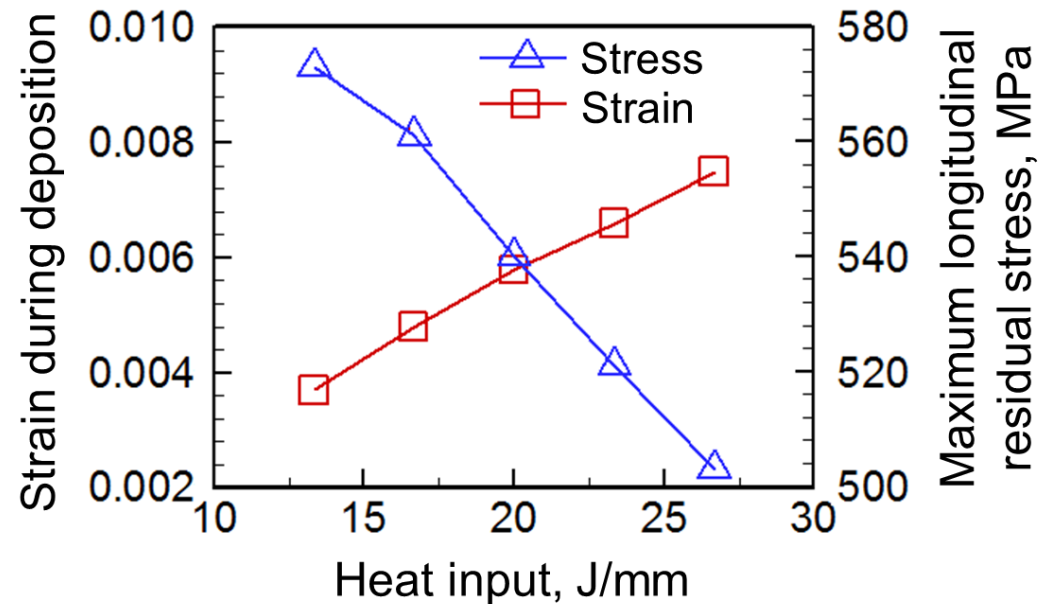
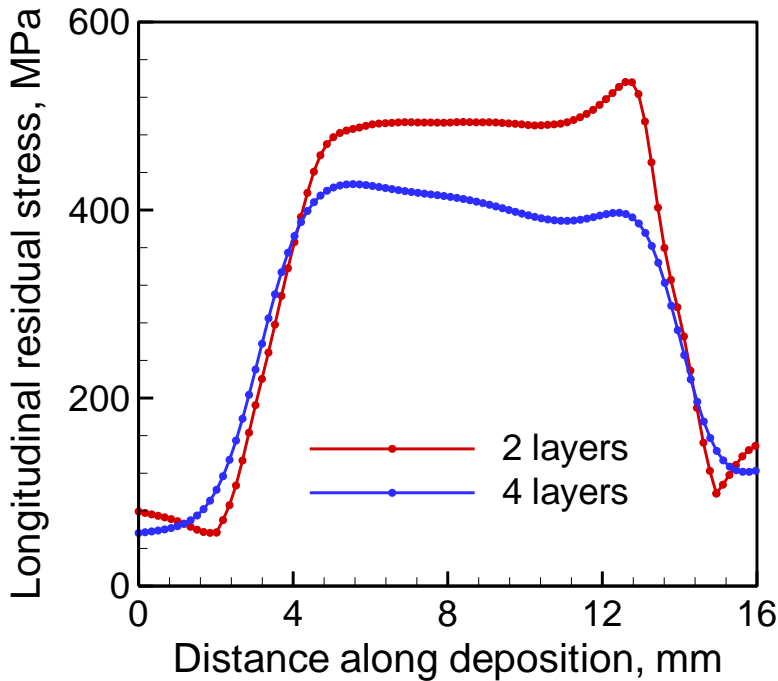
- ⇒ Time 't' is after the end of deposition
- ⇒ Longitudinal stress along the path may cause buckling and warping
- ⇒ Alloy: Inconel 718, Laser power: 300 W, Speed: 15 mm/s

Experimental validation of residual stresses



- => Experimental data are from [Shah et al. Sci. World J. 2014](#)
- => Laser power: 600 W, Speed: 4 mm/s
- => Slight mismatch could be caused by the measurement difficulty and the modeling assumptions

Effects of layer thickness and heat input

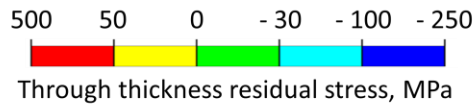
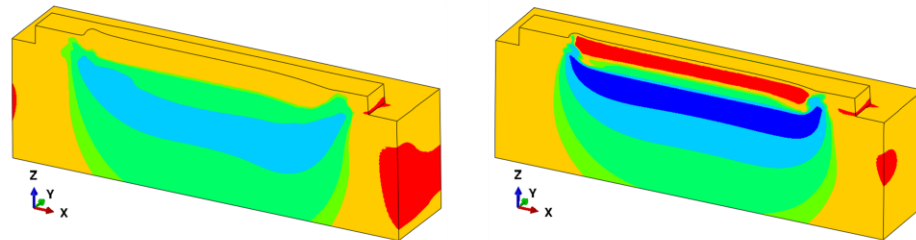
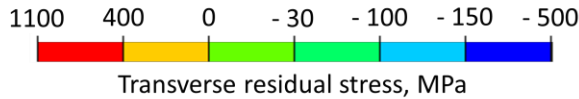
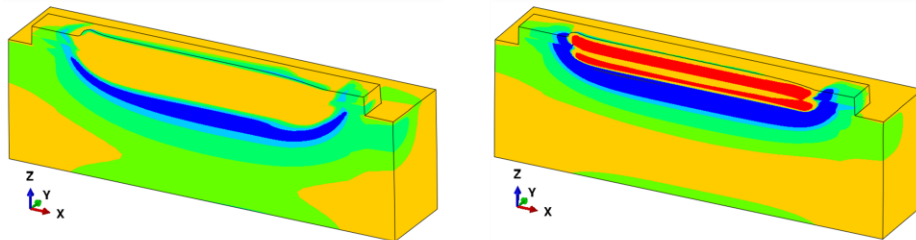
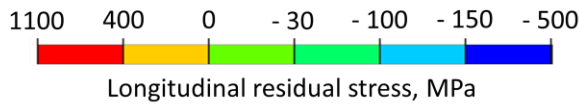
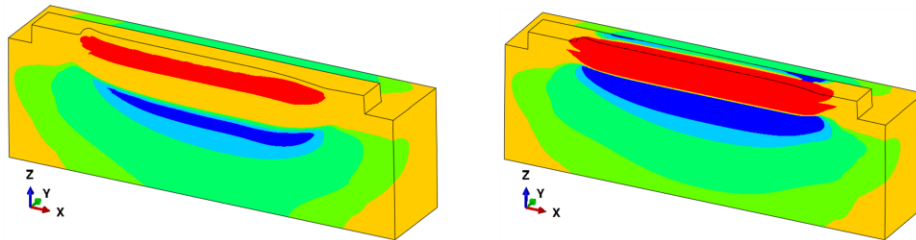


- => Residual stresses can be decreased as much as **30%** by **doubling** the number of layers to build the same height.
- => **Doubling** the heat input reduces the residual stresses by about **20%** and enhances the distortion by about **2.5 times**.
- => An appropriate heat input should be selected by **trading off** both distortion and residual stresses.

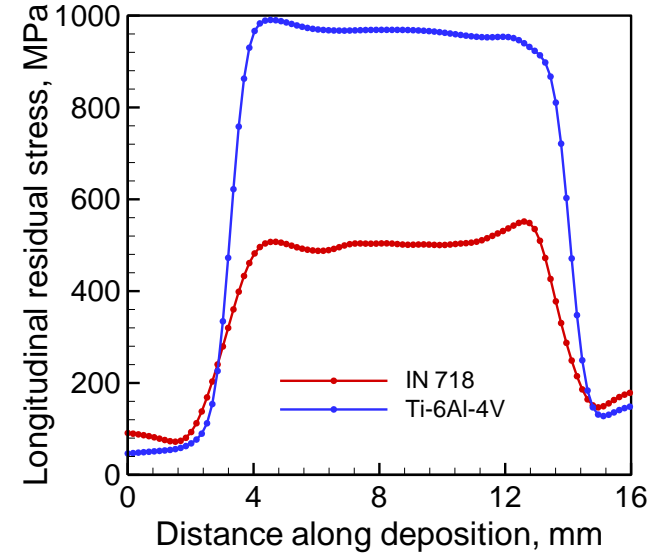
Residual stresses: Inconel 718 vs Ti-6Al-4V

Inconel 718

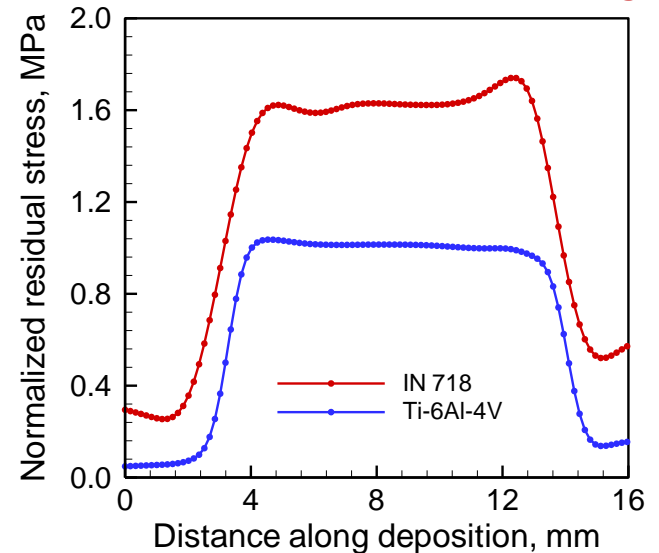
Ti-6Al-4V



Laser power: 600 W, Speed: 4 mm/s



$$\text{Normalized stress} = \frac{\text{Residual stress}}{\text{Yield strength}}$$

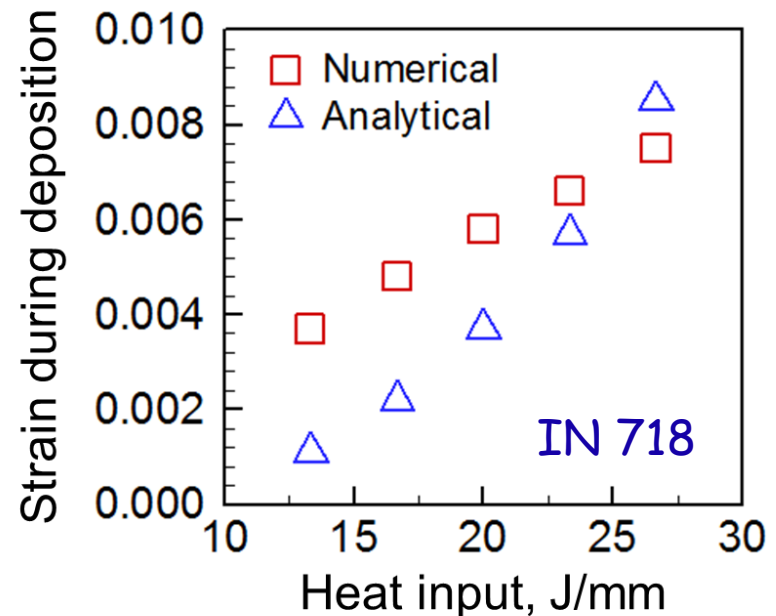
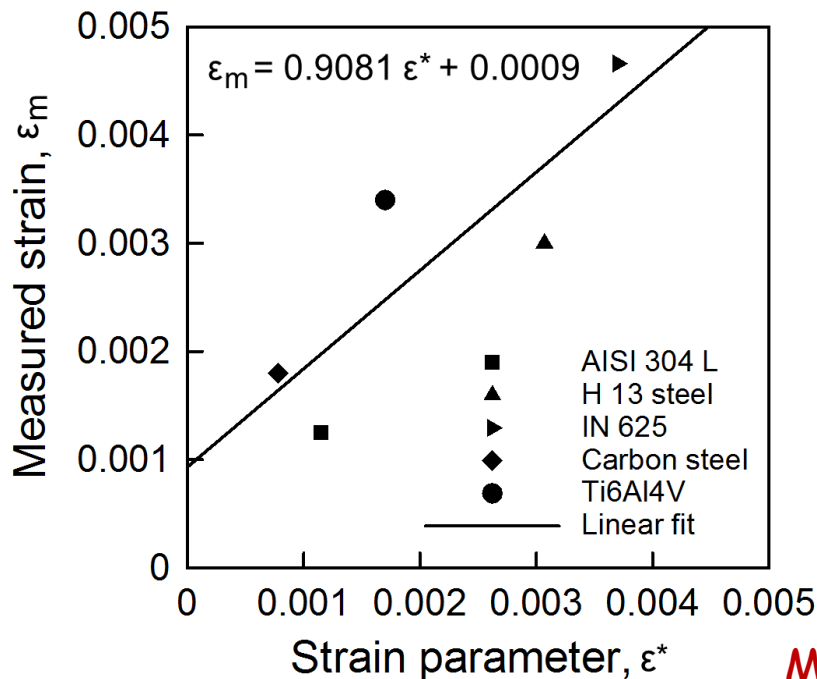


Measure of thermal distortion: Strain parameter

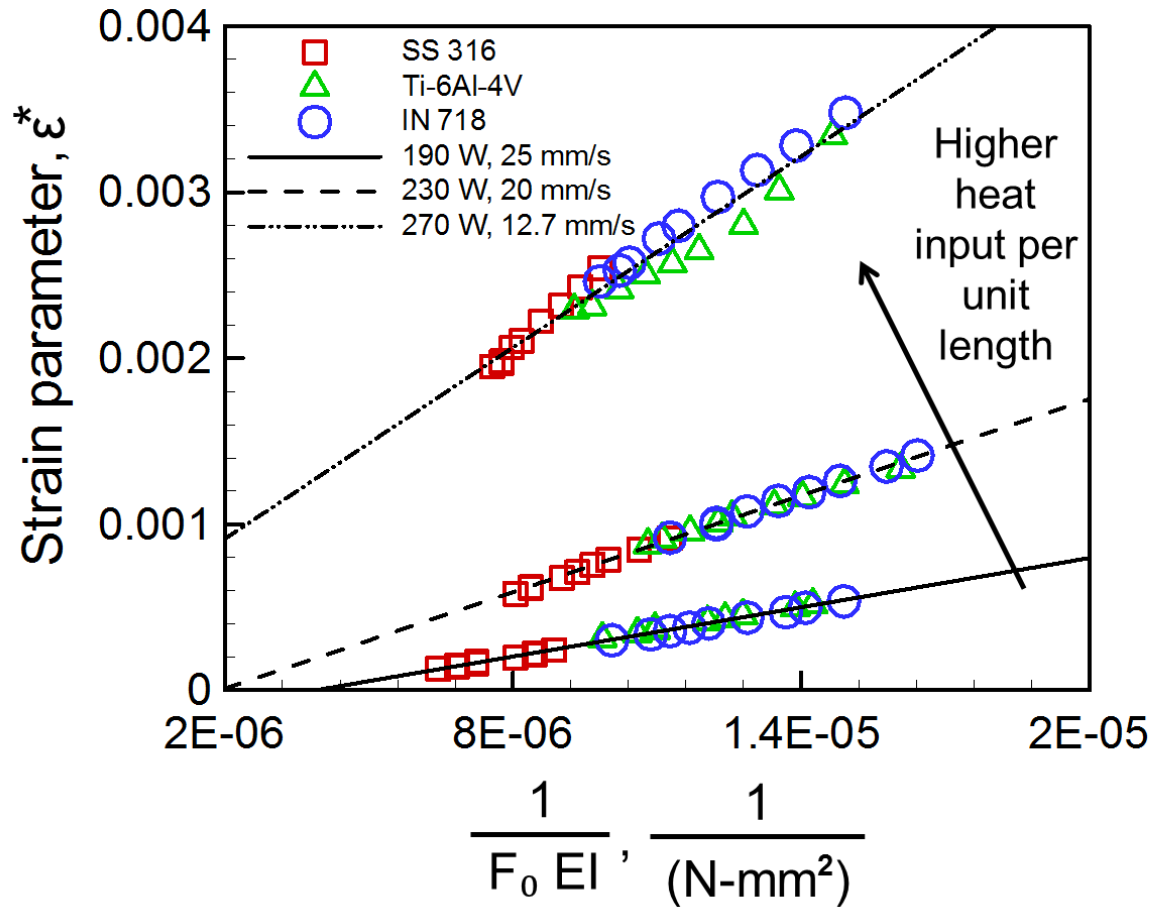
$$\varepsilon^* = \frac{\beta \Delta T}{EI} \frac{t}{F \sqrt{\rho}} H^{3/2}$$

- ε^* is obtained by dimensional analysis
- ε^* provides insight to thermal strain and distortion in AM
- ε^* does not consider any plastic deformation

Variables	Symbols
Thermal expansion coefficient	β
Temperature difference	ΔT
Fourier number	F
Heat input per unit length	H
Total time	t
Flexural rigidity of substrate	EI
Density	ρ



Thermal strain vs. Fourier number



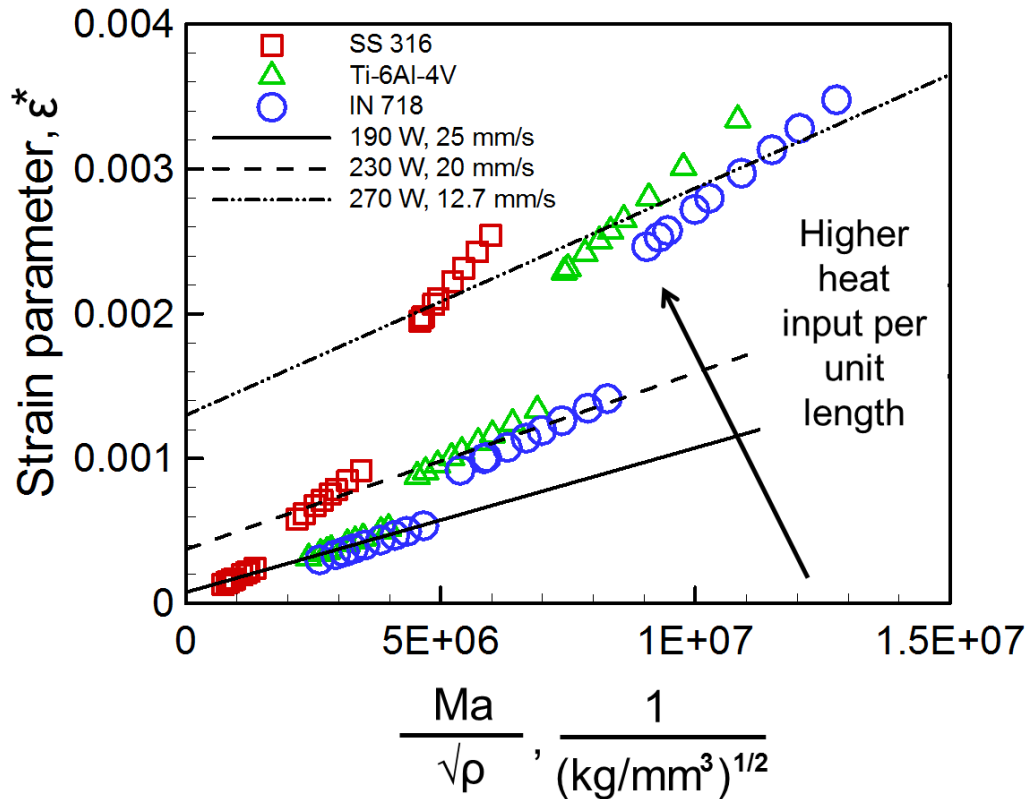
Fourier number (Fo) =
Heat dissipation rate
 Heat storage rate

EI = Flexural rigidity of
 the substrate

$$\varepsilon^* = \frac{\beta \Delta T}{EI} \frac{t}{F \sqrt{\rho}} H^{3/2}$$

- Low Fo \Rightarrow High heat storage \Rightarrow High thermal strain and distortion
- Low EI \Rightarrow Less rigid substrate \Rightarrow High thermal strain and distortion

Thermal strain vs. Marangoni number



Marangoni number =

$$Ma = - \frac{d\gamma}{dT} \frac{L\Delta T}{\eta\alpha}$$

Variables	Symbols
Surface tension gradient	$d\gamma/dT$
Pool length	L
Temperature gradient	ΔT
Viscosity	η
Thermal diffusivity	α

$$\varepsilon^* = \frac{\beta\Delta T}{EI} \frac{t}{F\sqrt{\rho}} H^{3/2}$$

- High Ma \Rightarrow High convective flow inside pool \Rightarrow Large pool \Rightarrow High strain
- Low density (ρ) \Rightarrow High peak temperature \Rightarrow High strain and distortion

Summary and conclusions

- ❖ A 3D transient heat transfer and fluid flow model is used to calculate the temperature field during the deposition.
- ❖ A thermo-mechanical model using Abaqus is used to simulate the residual stress and distortion.
- ❖ Lower layer thickness and heat input selected by trading off both distortion and residual stresses are useful to fabricate dimensionally accurate part with minimum residual stress.
- ❖ Non-dimensional strain parameter is used to understand the relative susceptibility to distortion of different alloys.
- ❖ High Fourier no. (high heat dissipation and low heat storage) and low Marangoni no. (less convective flow inside pool) can effectively reduce thermal distortion.